

1. Create a program which calculates the average of  $N$  random numbers taken from a uniform random number distribution. The program must run for  $N = 10, 100, 1000, 10000, 100000, 1000000$  random numbers. Plot the mean value as a function of  $N$  (axis of  $N$  should be logarithmic). Describe your conclusions. As initial seed use your record number (as in all the following exercises).

2. Create a program which performs a random walk for  $N = 1000$  steps. You will do that for two cases: **(a)** a one dimensional system, **(b)** a two dimensional system. The program should calculate the square displacement  $R^2$ . Run the program for 10000 runs and find the mean square displacement, namely  $\langle R^2 \rangle$ .

3. Use the program in the previous exercise to find the same thing, i.e.  $\langle R^2 \rangle$  but now every 100 steps, from 0 to 1000. You will perform 10000 runs and find 10 points (one every 100 steps), of which every point will be the average of 10000 runs. Plot your results, namely  $\langle R^2 \rangle$  vs. time. Use the least squares method as a fitting method to find the best straight line and the slope. Describe your conclusions.

4. Create a program which performs a random walk for  $N = 1000$  steps in one dimension. Calculate the displacement  $R$  for these  $N$  steps and perform 100.000 runs. Find the mean displacement  $\langle R \rangle$ . Find the distribution of  $R$ . Do the same for  $N = 500$  steps and find the distribution as well. Plot the distributions for both  $N$  values in the same graph. What are your conclusions from the two curves?

5. In the file [stud\\_grades.dat](#) are the grades of 10000 students who took an exam in a class. The grade range is from 0 to 20.

- a. Create a histogram where x-axis represents the grades in integer values and y-axis represents the frequency for each grade.
- b. Create a second histogram where x-axis represents the grades in decimal values of 1 digit precision and y-axis represent the frequency for each grade. (If a grade belongs in the interval  $[17.95, 18.04]$  then it is stored as 18.0, if it belongs in the interval  $[18.05, 18.14]$  it is stored as 18.1 etc)
- c. Calculate the mean value of the distribution
- d. Calculate the standard deviation of the distribution

6. Create a program which generates a 2 dimensional lattice of size 1000 x 1000. In this lattice place at random positions a number of trap molecules with concentration  $c$ . Place one particle at a random position on the lattice and let it perform a random walk as in the previous exercises. In this walk you will not place a time restriction, i.e. you will not declare a specific number of steps. The walk will stop when the particle falls on a trap. The time required for this is the trapping time. Perform 100000 runs, save the trapping times and make the distribution of these times.

Beware of boundary conditions. When the particle reaches the borders of the lattice it shouldn't be allowed to fall outside but to remain in the lattice, either by returning on its former position or by being placed in the opposite site of the lattice.

Run this program for  $c = 10^{-2}$  and  $10^{-3}$ . Put both distributions on the same graph. Describe your conclusions.